

IFAE, Pavia,
19 Aprile 2006

Cosmologia e neutrini, con massa fissa e variabile

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(Yale)

reviews:

Lesgourgues, Pastor astro-ph/0603494,
Giunti et al., Phys.Rept.379 hep-ph/0211462
Dolgov, Phys.Rept.370 hep-ph/0202122

MaVaNs:

Fardon, Nelson, Weiner JCAP 0410 (2004)
Cirelli, Gonzalez-Garcia, Pena-Garay NPB 2005
+ many others

OUTLINE

Part (1): **Neutrino masses and cosmology**: bird's eye view

- current bounds
- future sensitivities

Part (2): **Mass Varying Neutrinos**:

- the basic idea
- constraints from solar neutrino physics
- future developments

Conclusions

Neutrinos in cosmology

are significant because:

- neutrinos are **a lot** (as abundant as photons)
- neutrinos are **hot**
main component of the **rel energy density**
that sets the **expansion rate** of the Universe
- but **not so hot**, they have a **mass**
they cool down at an interesting time
- undergo **matter effects** in the primordial plasma
- determine **neutron/proton** in BBN,
i.e. primordial composition of the Universe
- have energy density similar to **Dark Energy**

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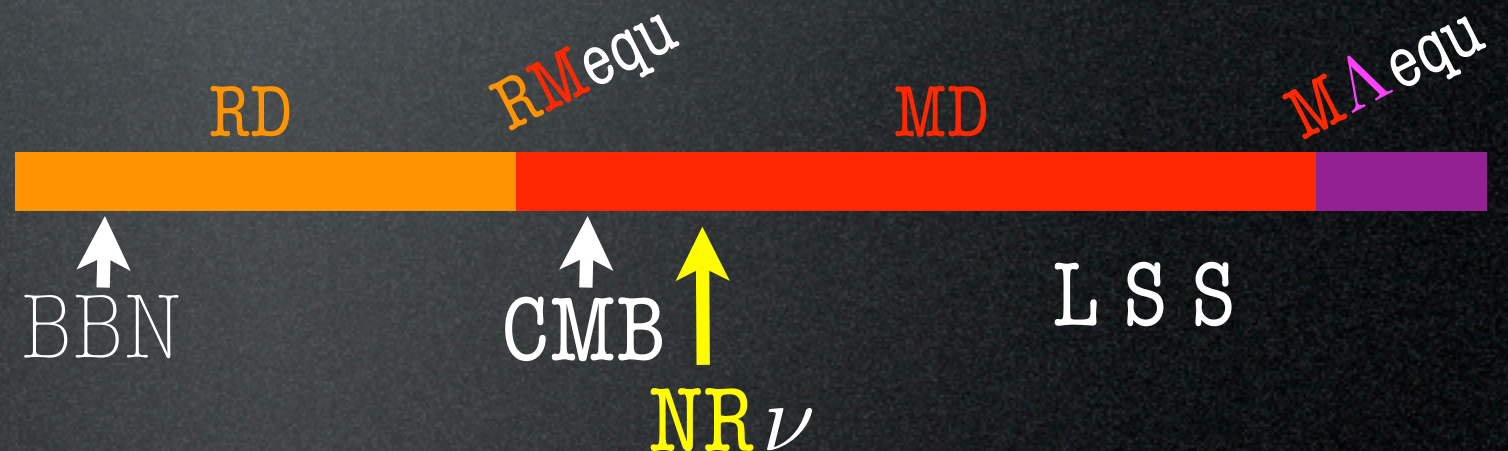
m_ν affects CMB and matter spectra

- Neutrinos become NR at $z \sim \frac{m_\nu c^2}{3 k T_{\nu,0}} \sim 2 \cdot 10^3 \left(\frac{m_\nu}{\text{eV}} \right)$

(CMB: $z \sim 1100$)

Since $m_\nu < 0.5 \text{ eV}$ $\left(\sum_i m_{\nu_i} < 1.5 \text{ eV} \right)$,

neutrinos became NR **after** CMB last scattering:



- **indirect** effect on CMB
- (indirect and) direct effect on LSS and later stuff

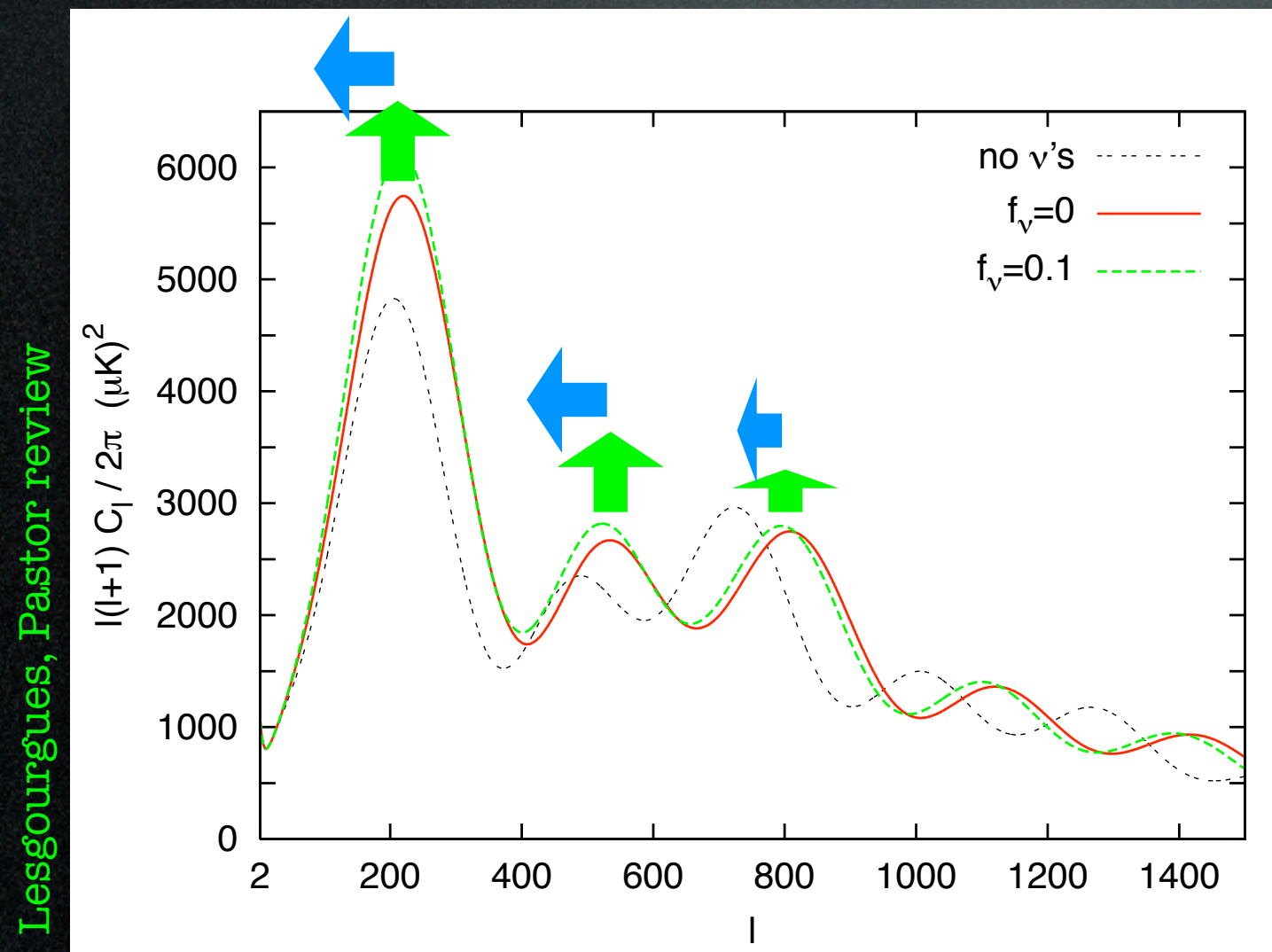
m_ν affects CMB and matter spectra

- On CMB power spectrum:

Contribution of neutrinos to the total energy density today

$$\Omega_\nu h^2 = \frac{\sum m_{\nu_i}}{93 \text{ eV}} \text{ at the expenses of other components, e.g. } \Omega_{\text{CDM}}$$

E.g. $m_\nu \nearrow$, $\Omega_\nu \nearrow$, $\Omega_{\text{CDM}} \searrow$, rel energy \nearrow , **RM** equ **delayed**.



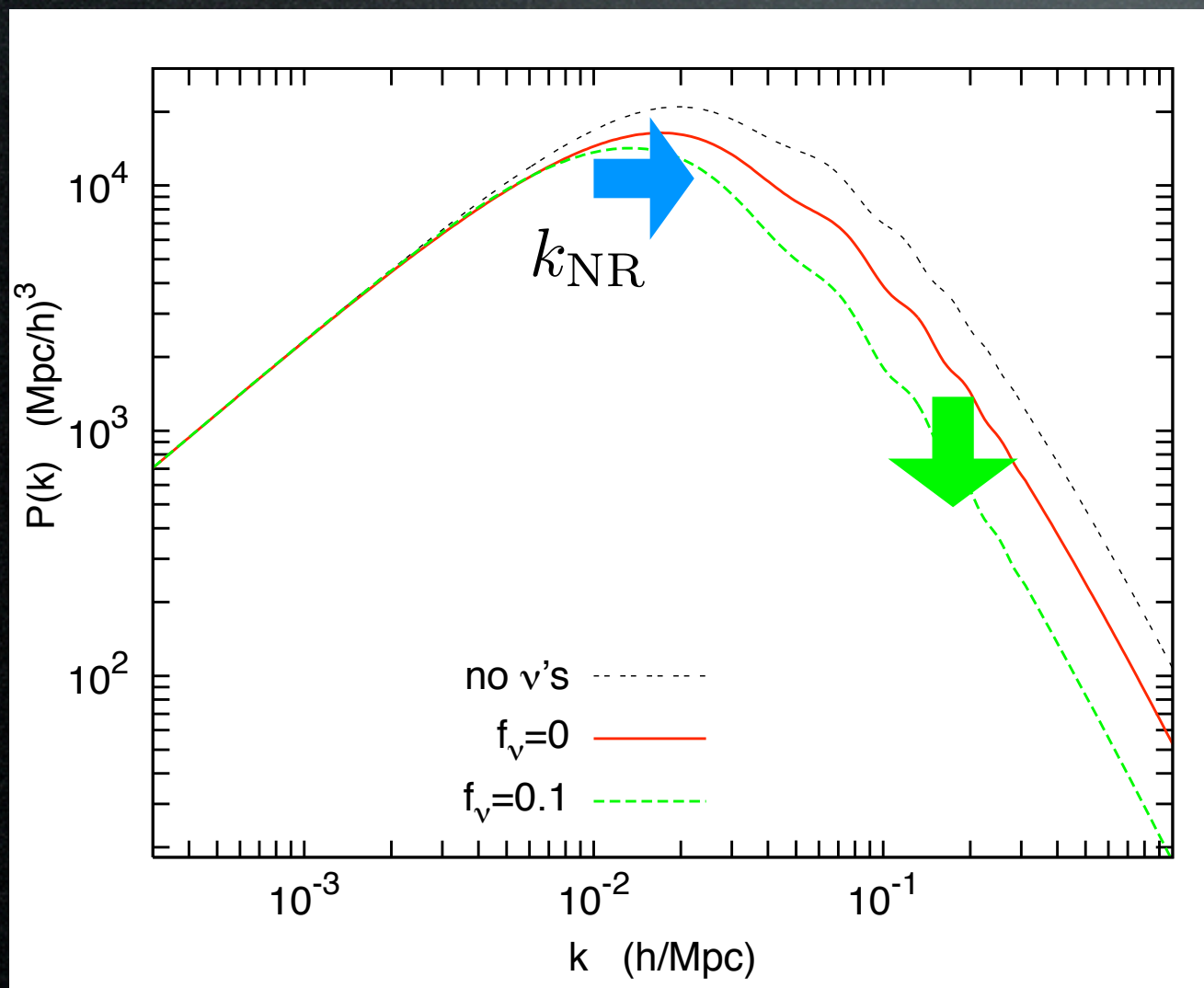
← the universe “was larger”
at recombination because
there was more RD

↑ less ISW effect right after
recombination because
grav wells decay more

Bottom line:
CMB spectrum is (mildly)
sensitive to $\sum m_{\nu_i}$.

m_ν affects CMB and matter spectra

- On matter power spectrum:
neutrinos are not trapped (**free stream**), counteracting the clustering of galactic structures.
Massive neutrinos become NR and travel $\lambda_{\text{FS}} < \text{Hubble radius}$.
Small scales are affected.



m_ν determines 2 things:

→ **time** (\leftrightarrow scale) of NR:

$$k_{\text{NR}} = 0.03 \left(\frac{m_\nu}{1 \text{ eV}} \right)^{1/2} \Omega_m^{1/2} h \text{ Mpc}^{-1}$$

$m_\nu \nearrow$, “slowed down” earlier,
could reach smaller scales

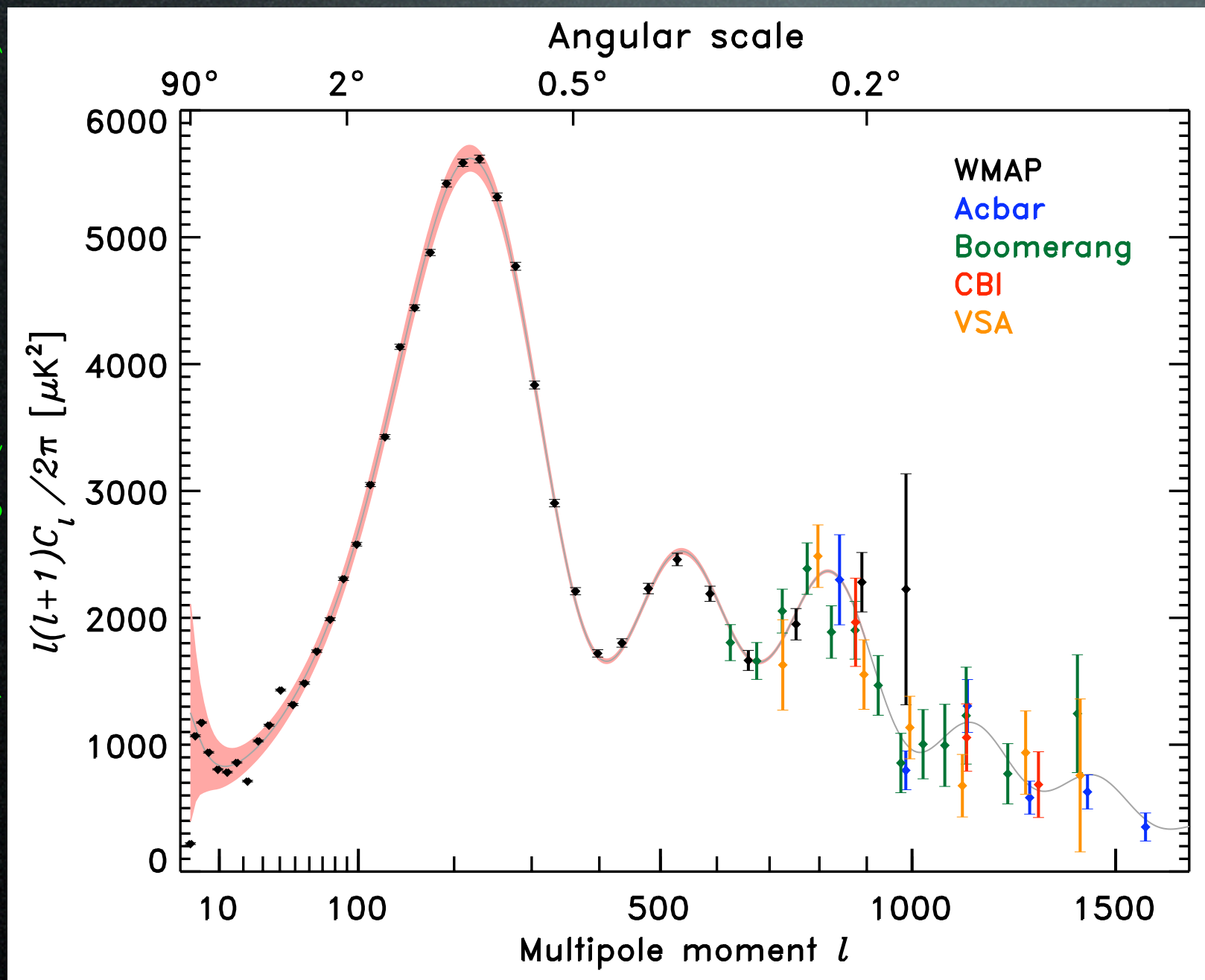
↓ **amount** of suppression:

$$\frac{\Delta P(k)}{P(k)} = -8 \frac{\Omega_\nu}{\Omega_m} \quad \Omega_\nu h^2 = \frac{\sum m_{\nu_i}}{93 \text{ eV}}$$

$m_\nu \nearrow$, $\Omega_\nu \nearrow$, suppression \nearrow

1. CMB alone

Hinshaw et al, WMAP 3yr (WMAP Science team)



Ichikawa et al. 2004

$$\sum m_{\nu_i} < 2.0 \text{ eV} \quad (95\% \text{ c.l.})$$

(WMAP 1yr + others)

WMAP 3yr, Spergel et al. 2006

$$\sum m_{\nu_i} < 2.11 \text{ eV}$$

(WMAP 3yr only)

Future:

e.g. Lesgourgues, Pastor 2004

$$\sum m_{\nu_i} \simeq \begin{pmatrix} 1.0 \\ 0.45 \\ 0.15 \end{pmatrix} \text{ eV} \quad (1\sigma)$$

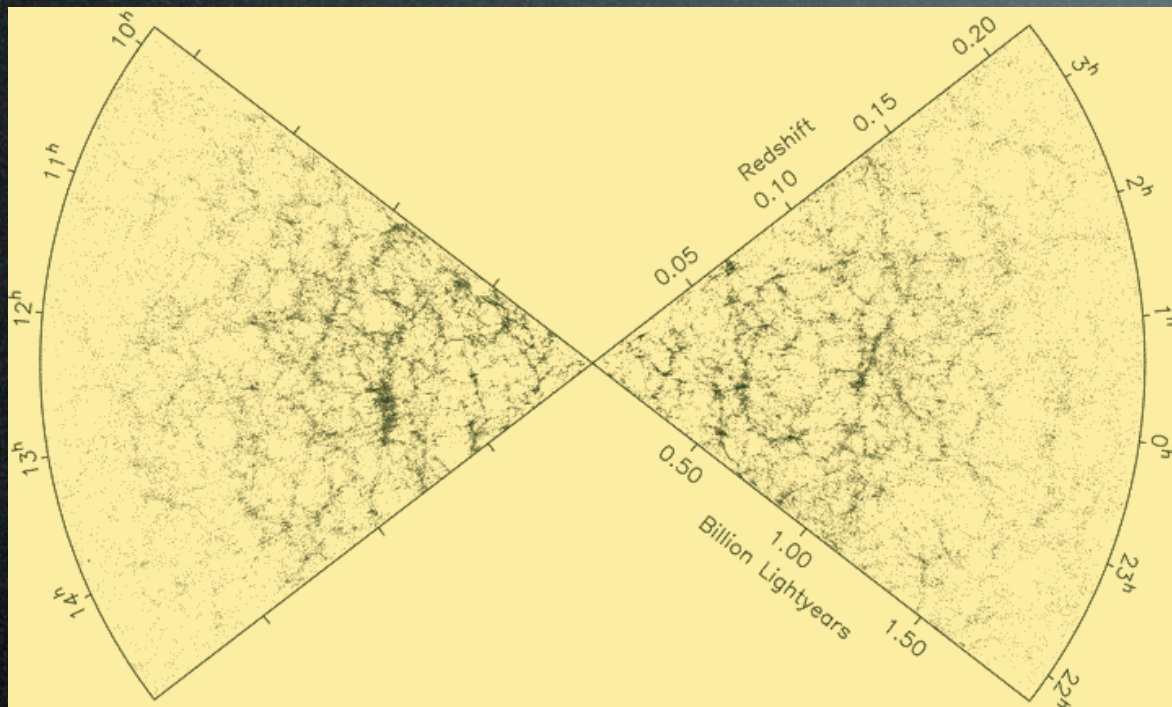
(future ground exp
Planck
CV limited)

Hannestad 2002

$$\sum m_{\nu_i} \simeq 0.07 \text{ eV}$$

2.LSS galaxy surveys

2dF GRS



2dF: completed, 222,000 galaxies
SDSS: on going, 5th data release, 1M galaxies

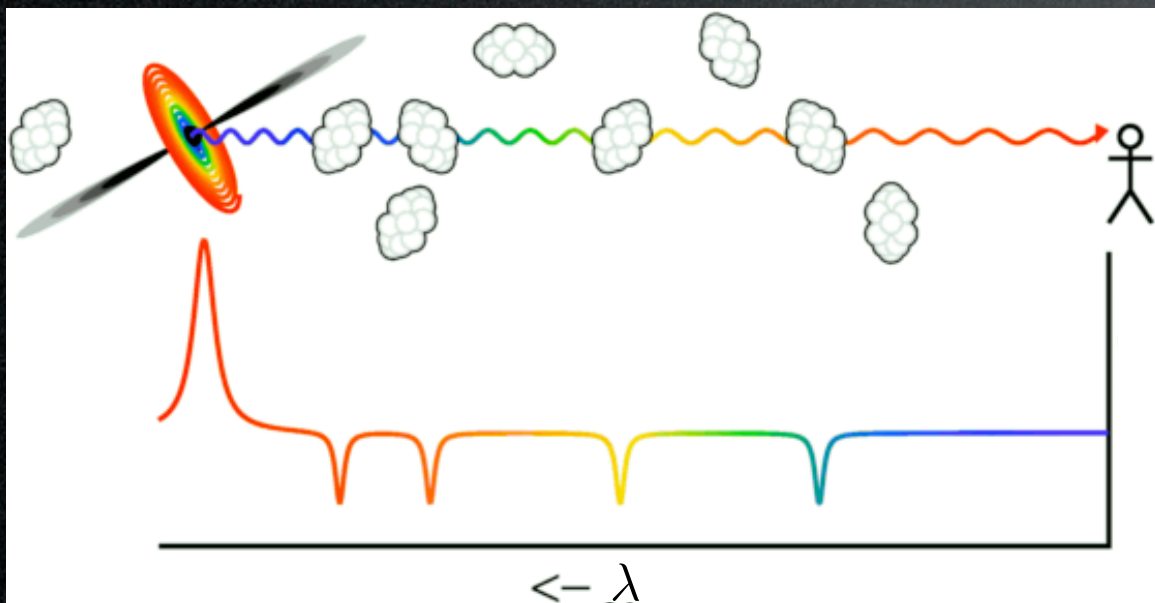
Redshift survey of galaxies allows to reconstruct matter distribution.

Bias parameter b :
how well does light of (non-lin evolved) galaxies trace matter distribution?

Simulations and direct measurements
say scale-indep and $b \approx 1.0 \pm 0.1$ Seljak et al., SDSS, astro-ph/0406594

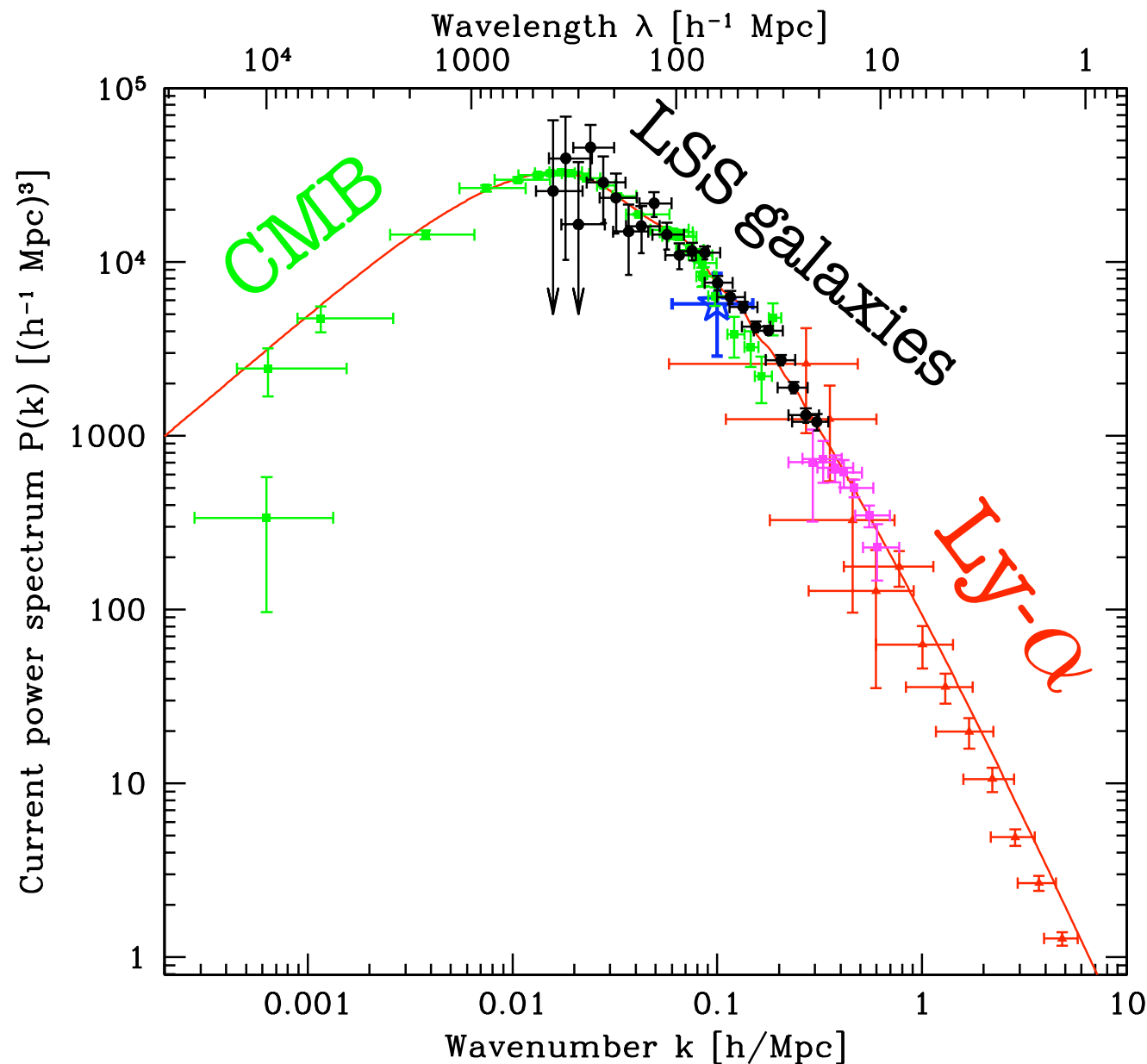
2b. Lyman-alpha forest

E. Wright, UCLA



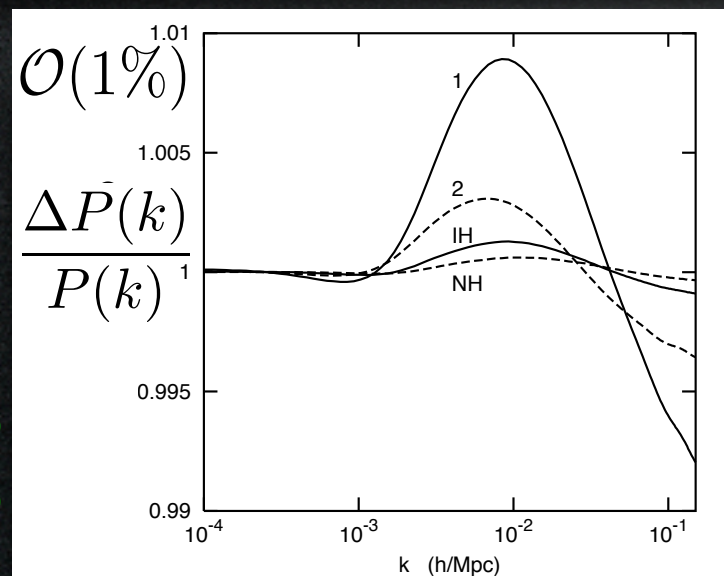
Distant quasar light, redshifted and absorbed at Ly- α frequency by intervening matter, allows to reconstruct matter z distribution along the line of sight.

But: systematics and uncertainties



Footnote:
is LSS sensitive
to Δm^2 ?
No, too small.

Lesgourgues et al. 2004



Issue (1): bias

Boomerang coll. 2005

$$\sum m_{\nu_i} < 1.2 \text{ eV}$$

no prior on b

$$\sum m_{\nu_i} < 0.48 \text{ eV}$$

 $b = 1.0 \pm 0.1$

Issue (2): Ly- α or not Ly- α ?

Fogli, Lisi et al. 2004

$$\sum m_{\nu_i} < 1.4 \text{ eV}$$

no Ly- α

$$\sum m_{\nu_i} < 0.47 \text{ eV}$$

with Ly- α

Issue (3): degeneracies/other data
HST, SNIa...

WMAP 3yr, Spergel et al. 2006

$$\sum m_{\nu_i} < 0.68 \text{ eV}$$

(WMAP 3yr + SDSS ($b = 1.03 \pm 0.15$) + 2dF (b margi'ed), **no Ly-a**)

Seljak et al. astro-ph/0604335

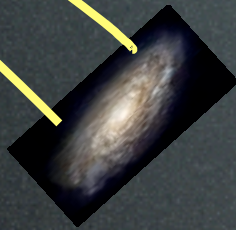
$$\sum m_{\nu_i} < 0.17 \text{ eV}$$

(WMAP 3yr + CMBall + SDSS + 2dF (free b) + SNIa + **Ly-a**)

Future: $\sum m_{\nu_i} \simeq 0.10 \text{ eV}$

Eisenstein, Hu, Tegmark 1998,
Lesgourgues, Pastor 2004(Planck + SDSS)
(CVlim + SDSS)

3.galaxy weak lensing



Weak lensing “**ellipticizes**” the image of background galaxies, allows to reconstruct intervening matter distribution.

Cooray, astro-ph/9904246

Future:

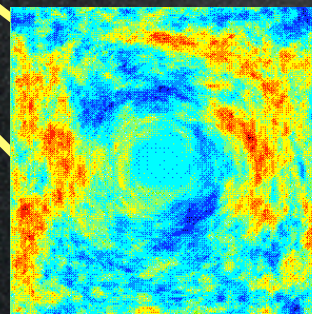
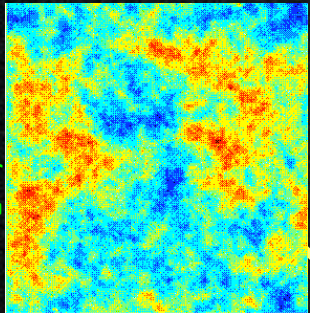
$$\sum m_{\nu_i} \simeq 0.1 \text{ eV}$$

$$\sum m_{\nu_i} \simeq 0.03 \text{ eV}$$

future lensing surveys:
DES, SNAP...

Song, Knox 2003

3.CMB weak lensing



Weak lensing “**distorts**” the CMB, allows to reconstruct intervening matter distribution.

Bernardeau, astro-ph/9611012, Seljak, Zaldarriaga, astro-ph/9810257

Future:

$$\sum m_{\nu_i} \simeq 0.4 \text{ eV}$$

(ground)

$$\sum m_{\nu_i} \simeq 0.15 \text{ eV}$$

(Planck)

$$\sum m_{\nu_i} \simeq 0.044 \text{ eV}$$

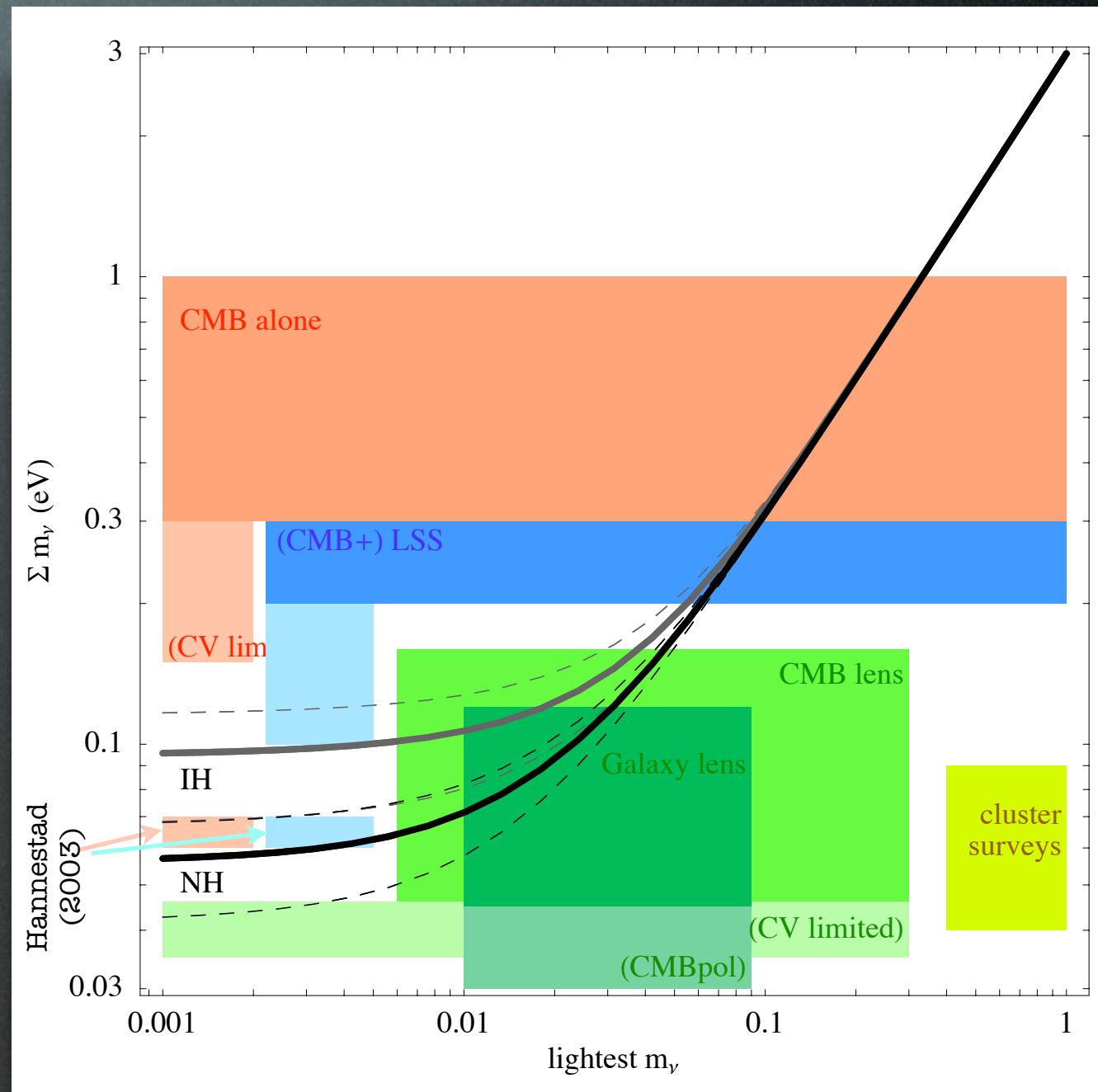
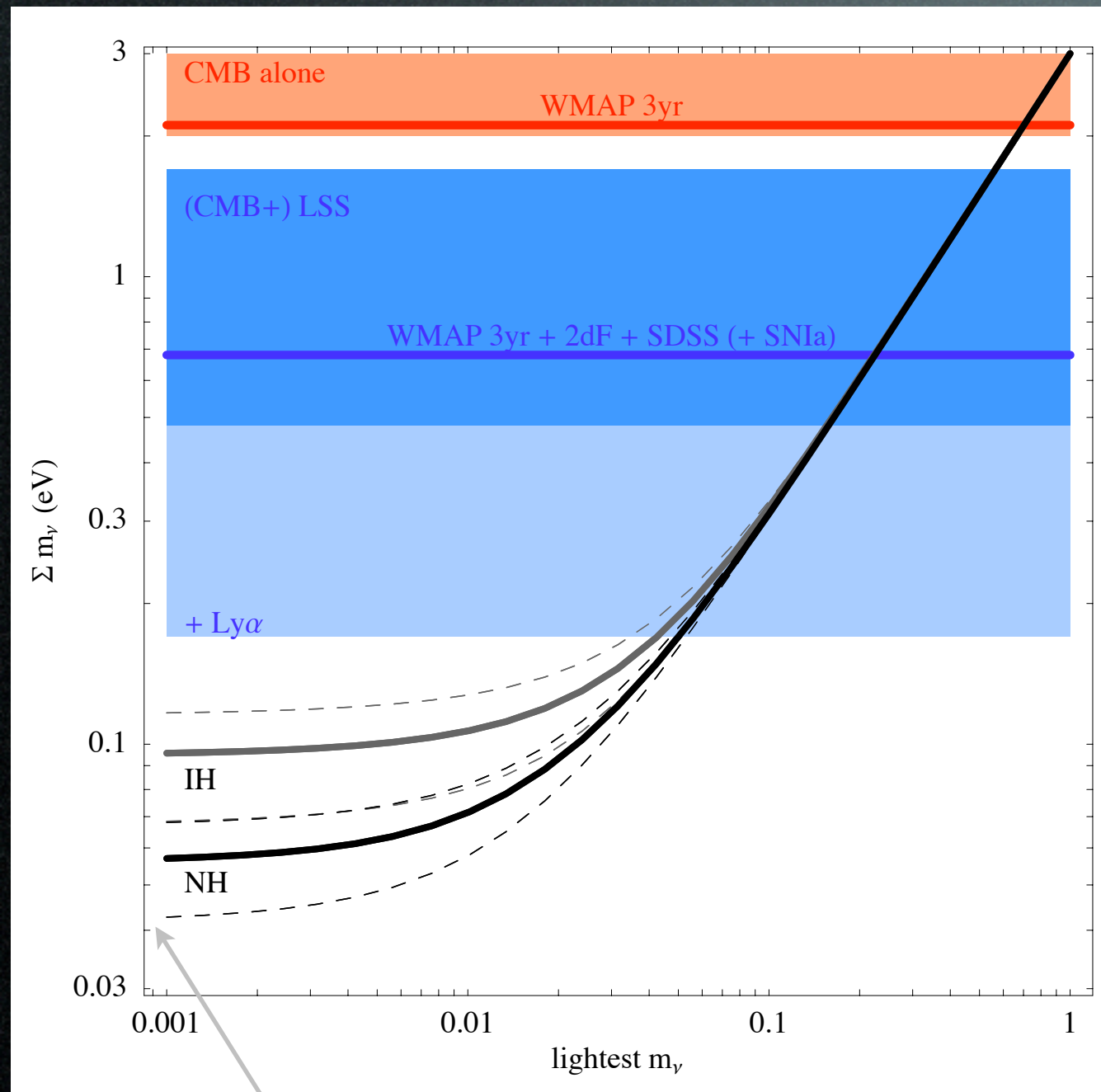
(CV limited)

Kaplinghat et al. 2003,
Lesgourgues, Pastor 2006

Summary

present bounds

future sensitivities



Legenda: the bound or measurement will fall somewhere in the colored box; "where it'll fall exactly" depends on the author, the experiment considered, priors, the weather...

Mass Varying Neutrinos

Fardon, Nelson, Weiner JCAP 0410 (2004)

Kaplan, Nelson, Weiner PRL93 (2004)

Zurek 2004

Peccei 2005

Bi, Feng, Gu, Li, Wang, Zhang 2003-4

Cirelli, Gonzalez-Garcia, Pena-Garay 2005

Horvat 2005

Afshordi, Zaldarriaga, Kohri 2005

Takahashi, Tanimoto 2005

Fardon, Nelson, Weiner 2005

Barger, Marfatia, Whisnant 2005

Weiner, Zurek 2005

Honda, Takahashi, Tanimoto 2005

Zhang 2005

Ichikawa, Takahashi 2005

Gu, Bi, Zhang 2005

Gonzalez-Garcia, de Holanda, Funchal 2005

Schwetz, Winter 2005

Gu, Bi, Feng, Young, Zhang 2005

Brookfield, van de Bruck, Mota, Tocchini-Valentini 2005

Mass Varying Neutrinos

Inspiration:

Fardon, Nelson, Weiner, JCAP 2004

- we don't understand **Dark Energy**, but it's there
we don't understand **neutrino mass**, but it's there
- they have a similar value and
they have a similar value today

$$\Omega_\Lambda = \frac{\rho_{de}}{\rho_c} \simeq 70\% \Rightarrow \rho_{de} \simeq 3 \cdot 10^{-11} \text{ eV}^4 \Rightarrow \sqrt[4]{\rho_{de}} \simeq 2 \cdot 10^{-3} \text{ eV}$$

$$m_\nu \simeq \sqrt{\Delta m_{atm}^2} = \sqrt{2 \cdot 10^{-3} \text{ eV}^2} = 5 \cdot 10^{-2} \text{ eV}$$
$$m_\nu \simeq \sqrt{\Delta m_{sun}^2} = \sqrt{7 \cdot 10^{-5} \text{ eV}^2} = 8 \cdot 10^{-3} \text{ eV}$$

$$\rho_{\nu,0} \simeq \sum m_{\nu_i} n_{\nu b,i} \simeq \text{few } 10^{-14} \text{ eV}^4$$

$$n_{\nu b,i} = \frac{3}{4} \frac{\zeta(3)}{\pi^2} g_\nu T_{\nu,0}^3 = 8 \cdot 10^{-13} \text{ eV}^3$$
$$\simeq 112 \text{ cm}^{-3}$$

- maybe they are related
maybe they “track” each other

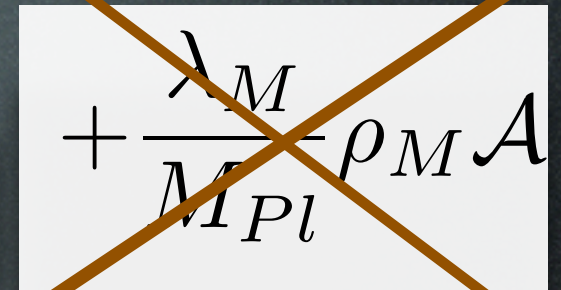
(A different approach:
Barbieri, Hall, Oliver, Strumia, 2005)

The framework:

Fardon, Nelson, Weiner, JCAP 2004

Ingredients ν_l \mathcal{A} N_r

$$\mathcal{L} = m_D \nu_l N_r + M(\mathcal{A}) N_r N_r + V_{tot}(\mathcal{A})$$


$$+ \frac{\lambda_M}{M_{Pl}} \rho_M \mathcal{A}$$

Barger et al. hep-ph/0502196

$$m_\nu(\mathcal{A}) = \frac{m_D^2}{M(\mathcal{A})} \quad (\text{“see-saw”})$$

$$\mathcal{L} = m_\nu(\mathcal{A}) \nu_l \nu_l + V_{de} + V_{c\nu b} + V_{\nu, \text{medium}}$$

$$V_{de} = V_{de}(m_\nu(\mathcal{A}))$$

$$V_{c\nu b} = m_\nu(\mathcal{A}) n_{c\nu b}$$

$$V_{\nu, \text{medium}} = \int \frac{d^3 k}{(2\pi)^3} \sqrt{k^2 + m_\nu^2} f(k)$$

neutrino energy

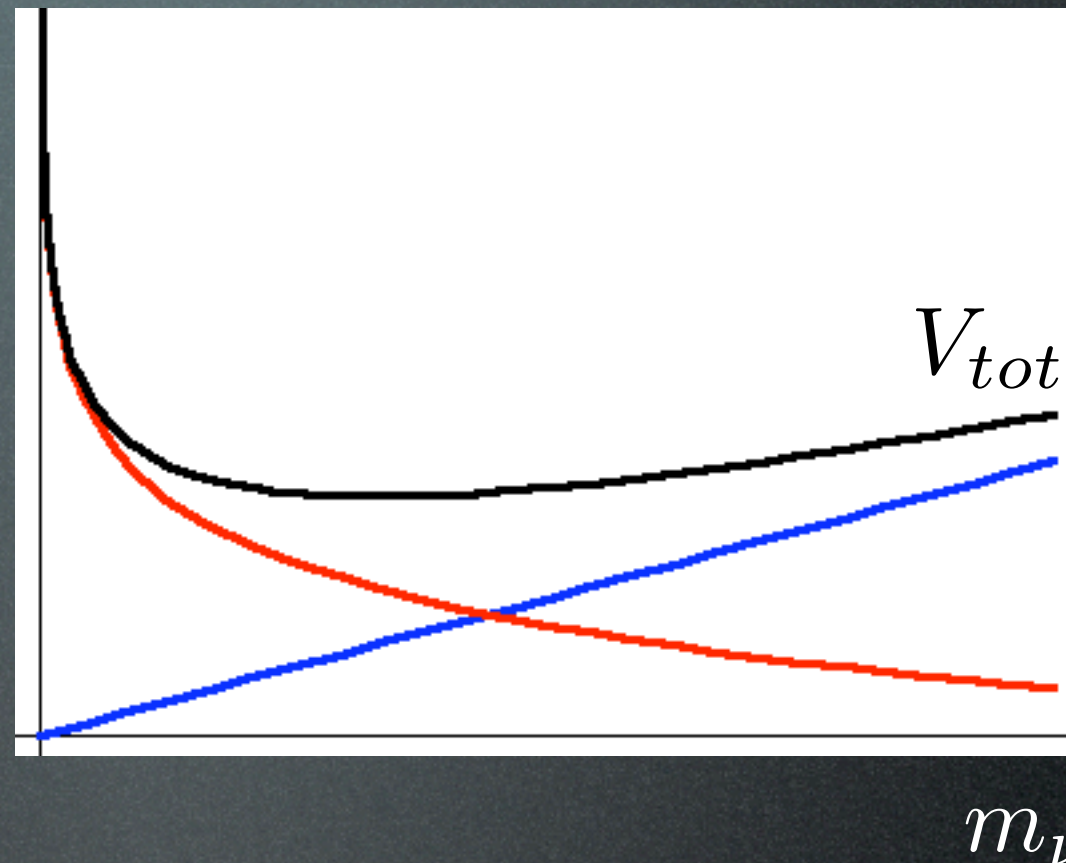
neutrino distribution fnct

In the “vacuum”:

$$V_{tot} = V_{de} + V_{c\nu b}$$

$$V_{c\nu b} = m_\nu(\mathcal{A}) n_{c\nu b}$$

$$V_{de} = \Lambda^4 \log\left(\frac{\mu}{m_\nu}\right)$$



$V_{c\nu b}$
 V_{de}
A quintessence potential.
No, it's not stable under
radiative corrections.

- $\Lambda \sim 10^{-3}$ eV
- $m_\nu \neq 0 \Rightarrow V'_{de}(m_\nu) < 0$
- $\omega \approx -1 \Rightarrow |V'_{de}(m_\nu)| \ll 1$ (flat DE potential) ($\omega = -0.97^{+0.07}_{-0.09}$)

WMAP 3yr

minimization of the total potential

$$\frac{dV_{tot}(m_\nu)}{dm_\nu} \equiv 0 \Rightarrow$$

$$m_{\nu,0} = \frac{\Lambda^4}{n_{c\nu b}}$$

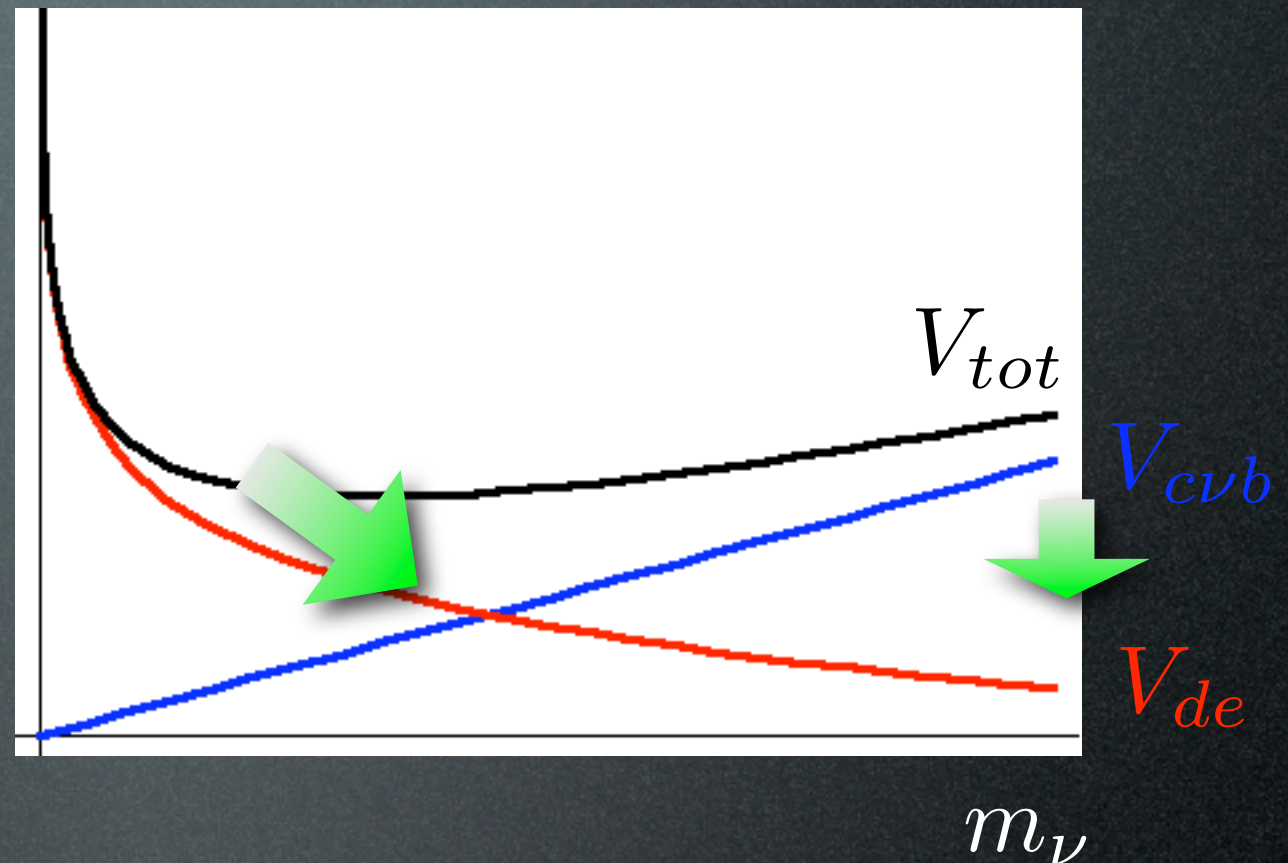
← mass
varying!

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$$m_{\nu,0} = \frac{\Lambda^4}{n_{c\nu b}}$$

← **mass
varying!**

In a neutrino rich medium:

$$V_{tot} = V_{de} + V_{c\nu b} + V_{\nu, \text{medium}}$$

$$V_{\nu, \text{medium}} = \int \frac{d^3 k}{(2\pi)^3} \sqrt{k^2 + m_\nu^2} f(k)$$

minimization of the total potential

$$\frac{dV_{tot}(m_\nu)}{dm_\nu} \equiv 0 \Rightarrow V'_{de}(m_\nu) + n_{c\nu b} + m_\nu \int \frac{d^3 k}{(2\pi)^3} \frac{1}{\sqrt{k^2 + m_\nu^2}} f(k) \equiv 0$$

$$m_\nu = m_{\nu,0} - A m_{\nu,0}^2 + \dots$$

- if $A \rightarrow 0$, back to vacuum case
- if $A \sim \mathcal{O}(1)$...

$$A = \frac{1}{n_{c\nu b}} \int \frac{d^3 k}{(2\pi)^3} \frac{1}{\sqrt{k^2 + m_\nu^2}} f(k) \approx \frac{1}{n_{c\nu b}} \frac{n_{\nu, \text{medium}}}{\langle E_\nu \rangle}$$

In the Sun:

given solar ν_e spectrum and prod regions, compute effective Δm^2

$$\begin{aligned} \Delta m_{\text{MaVaN}}^2(x) &= m_2^2(x) - m_1^2(x) \\ &\simeq \Delta m_0^2 [1 - 3A_2(x)m_{01}] + 2[A_1(x) - A_2(x)]m_{01}^3 + \dots \end{aligned}$$

effective Δm^2 is a function of m_{01} !

Solar + KamLAND fit: results

-fit worsens with m_{01}
(best fit for $m_{01} = 0$)

-Solar only:

- moves to lower $\Delta m_{21,0}^2$
- but D/N asymmetry
- and CC/NC ratio

-Solar + KamLAND:

- KamLAND nails $\Delta m_{21,0}^2$ high



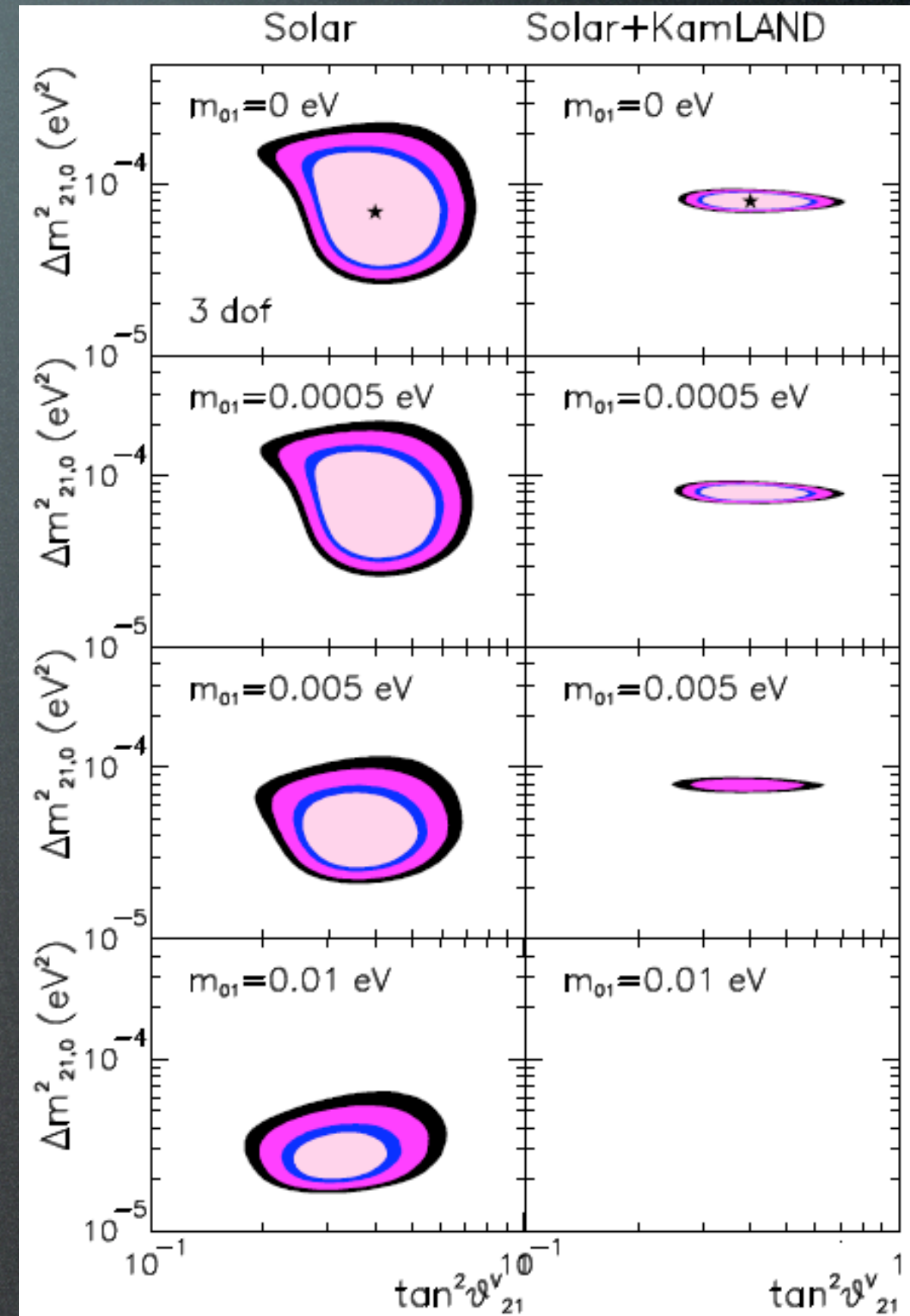
upper bound on m_{01} :

solar only

$$m_{01} \lesssim 0.05 \text{ eV}$$

solar + KamLAND

$$m_{01} \lesssim 0.01 \text{ eV}$$



[more results]

Outlook:

MaVaNs clustering:

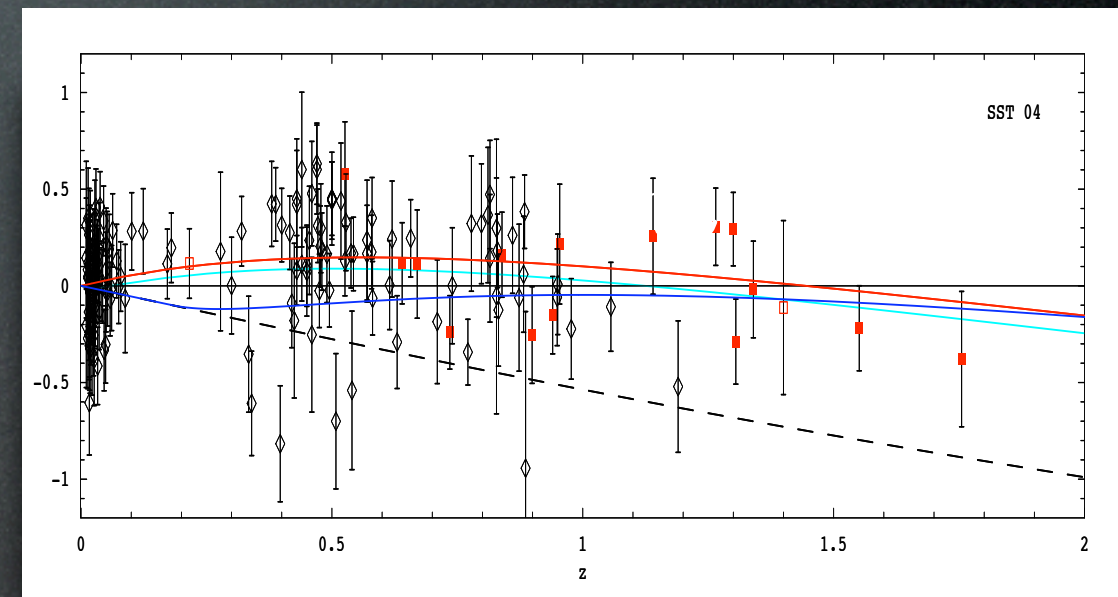
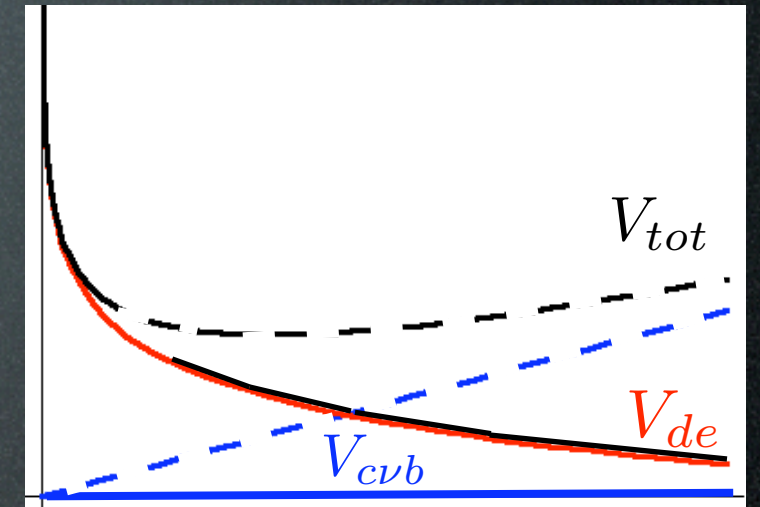
when ν become NR, instabilities collapse,
neutrino CDM-like nuggets form.

- connection with m_ν^{today} lost
- DE disappears (SNIa data uproar)

alternatively:

- only the lightest neutrino, still R, is coupled to DE?
- clustering occurred yesterday?
(indistinguishable from Λ ?)

Afshordi, Zaldarriaga, Kohri 2005



Couple to **ordinary matter**, environmental mass:

- does *not* reconcile LSND
- effects on solar and reactor and accelerator neutrinos...

Conclusions

- the bound from cosmology is the **dominant bound** on m_ν :

CMB only

(CMB +) LSS

+ Ly- α

$$\sum m_{\nu_i} < 2.11 \text{ eV}$$

$$\sum m_{\nu_i} < 0.68 \text{ eV}$$

$$\sum m_{\nu_i} < 0.17 \text{ eV}$$

(status on 19 april 2006)

- future improvements likely “**guarantee**” positive detection (e.g. lensing surveys)
- **Mass Varying Neutrinos** models aim to link fruitfully neutrinos and DE: work in progress

solar + KamLAND physics imply

$$m_{01} \lesssim 0.01 \text{ eV}$$

Extra slides

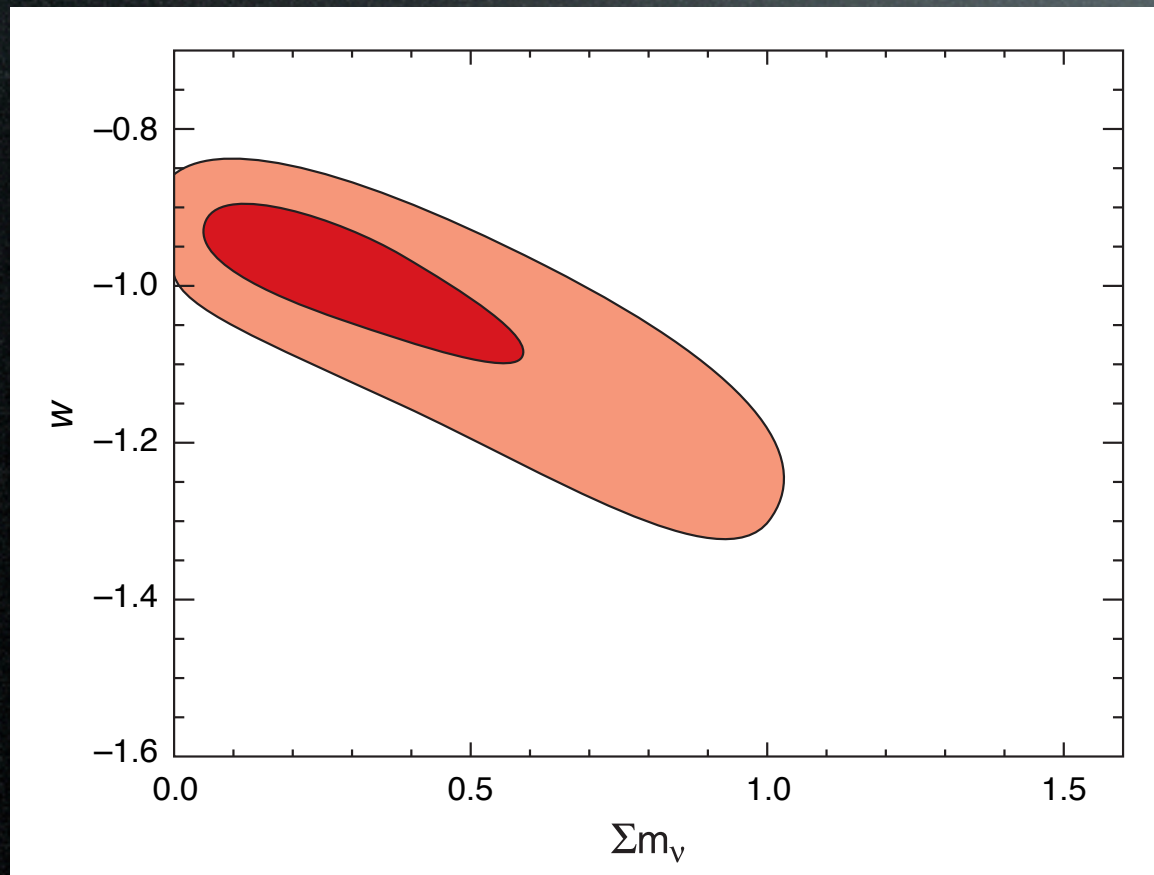
LSS and degeneracies

m_ν effect can be cancelled
by $w < -1$.

Hannestad,
astro-ph/0505551

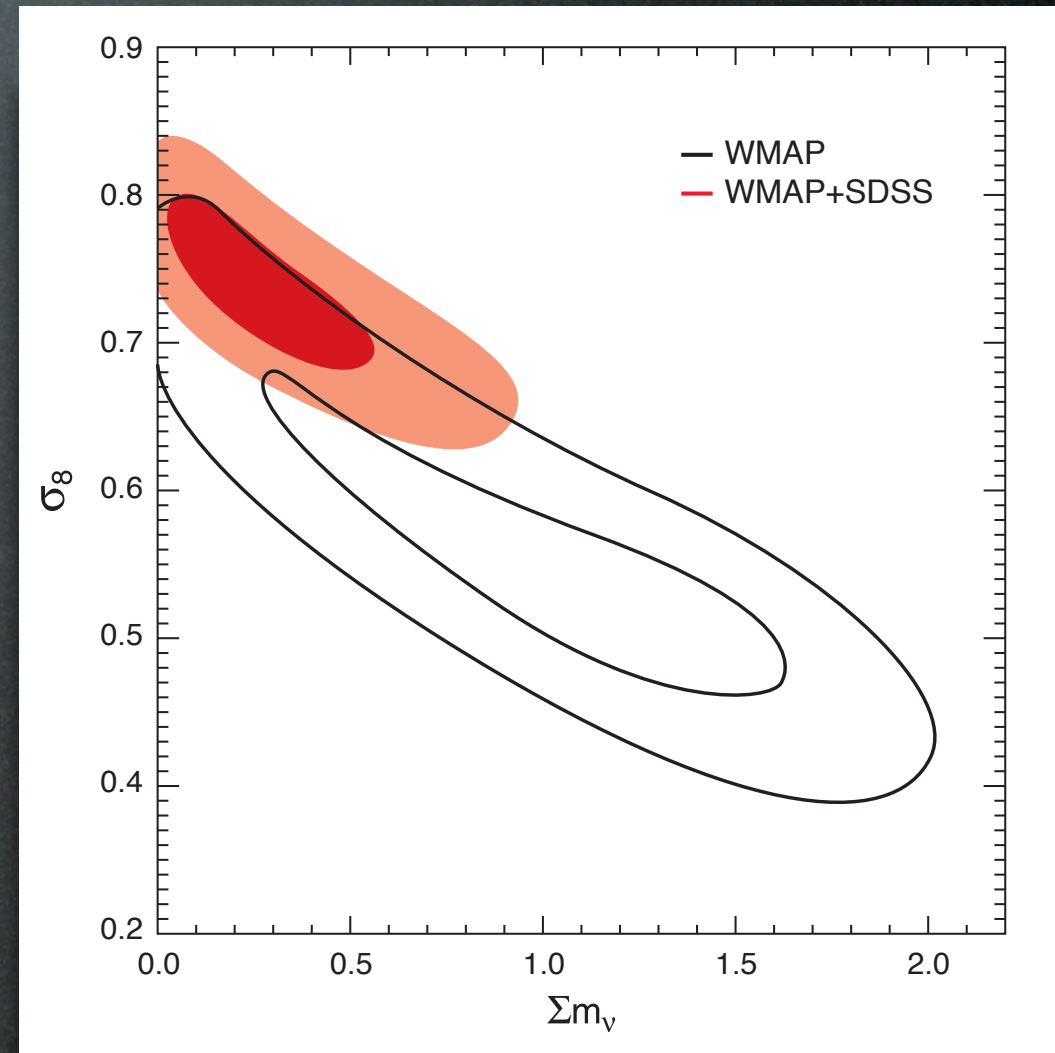
(SNIa data allow less Ω_Λ , hence more Ω_m ,
if $w < -1$; more Ω_m brings back up the $P(k)$)

WMAP 3yr, Spergel et al.



Still, $\Sigma m_{\nu_i} \lesssim 1.0$ eV.

m_ν effect can be cancelled
by low σ_8 .



[back to LSS]

more on MaVaNs results

(in order of boldness)

- upper bound on m_{01} :

solar only

$$m_{01} \lesssim 0.05 \text{ eV}$$

solar + KamLAND

$$m_{01} \lesssim 0.01 \text{ eV}$$

(3 σ)

- lower bound on “degeneracy param.” $\frac{\Delta m_{21,0}^2}{m_{01}^2}$:

solar only

$$\frac{\Delta m_{21,0}^2}{m_{01}^2} > 2 \cdot 10^{-2}$$

solar + KamLAND

$$\frac{\Delta m_{21,0}^2}{m_{01}^2} > 1$$

(3 σ)

i.e. inverse hierarchy not likely $m_{01} \simeq \sqrt{\Delta m_{\text{ATM}}^2} \simeq 0.06 \text{ eV}$

- when m_{01} known, $\Delta m_{\text{MaVaNs}}^2$ known \Rightarrow proof-test MaVaNs

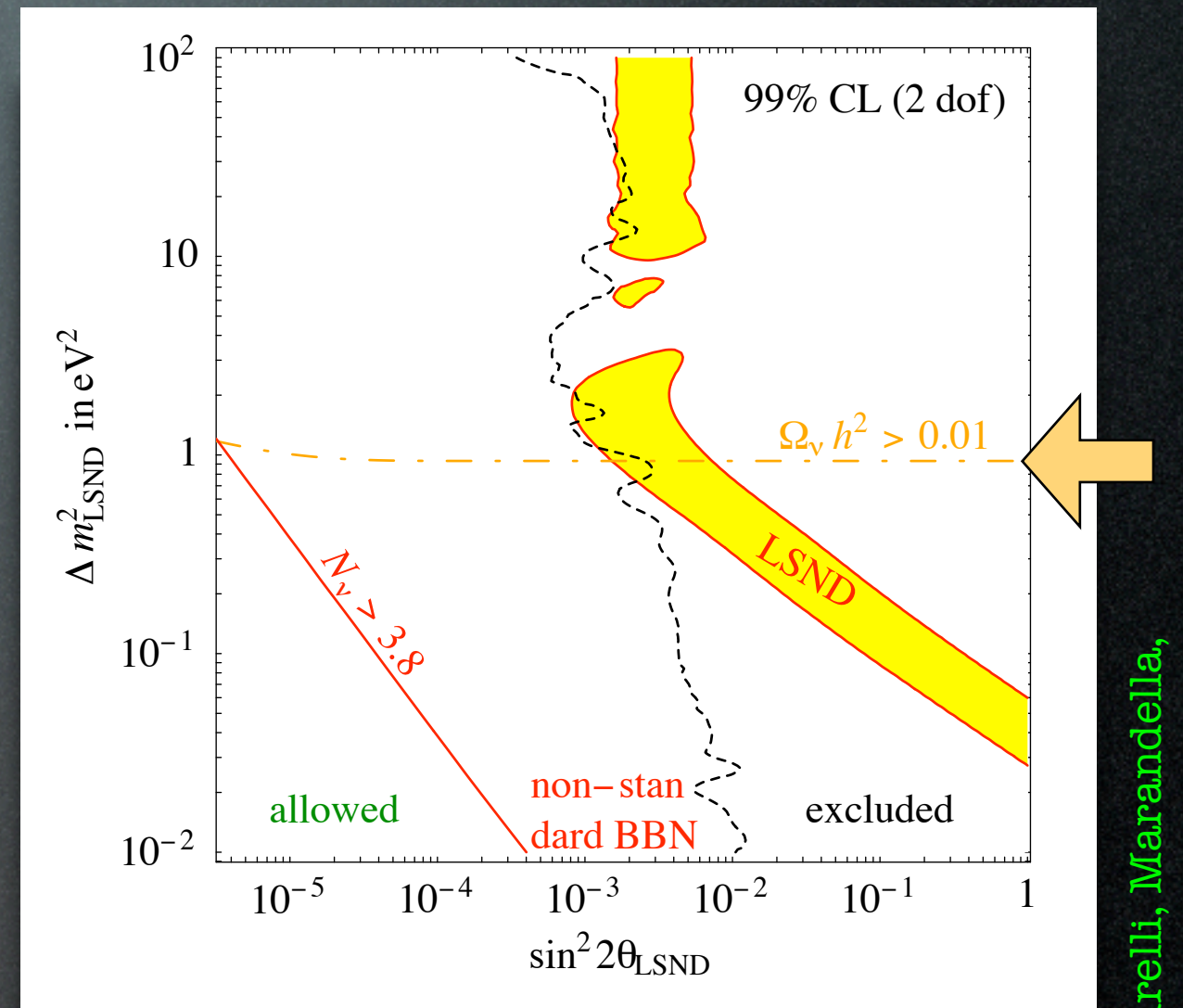
- if $\Delta m_{\text{eff,sol}}^2 \neq \Delta m_{\text{KamLAND}}^2 \Rightarrow$ determined m_{01} with oscillation experiments!

LSND sterile and the cosmological mass bound

If a 4th (sterile) neutrino exists, the bound applies:

$$\Omega_\nu h^2 = \frac{\text{Tr}[m \cdot \rho_\nu]}{93 \text{ eV}} \rightarrow \frac{\sum m_{\nu_i}}{93 \text{ eV}}$$

(in the limit of fully thermalized extra state)



LSND neutrino almost excluded.

Neutrinos cosmology in one sentence! Wow...

??

CnuB

Sun, SNe

Nature provides for three types of neutrinos, yet scientists know very little about these "ghost particles," which can traverse the entire Earth without interacting with matter. But the abundance of neutrinos in the universe, produced by stars and nuclear processes, may explain how galaxies formed and why antimatter has disappeared. Ultimately, these elusive particles may explain the origin of the neutrons, protons and electrons that make up all the matter in the world around us.

Reactors

BBN

LSS

Leptogenesis

MINOS press release, march 2006